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Wave energy converter configuration in dual wave farms

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Abstract

Wave farms, i.e., arrays of Wave Energy Converters (WECs), have recently been proven to be effective in fulfilling the dual function of carbon-free energy generation and coastal protection. In this paper these dual-function wave farms are referred as dual wave farms. The objective of this work is to investigate the influence of the WEC configuration on the performance of these dual wave farms through a case study: a dual wave farm consisting of WaveCat WECs deployed off an eroding beach. WaveCat is a floating overtopping WEC consisting of two hulls joined by their stern, forming a wedge. Two configurations are considered, with wedge angles of 30° and 60° . To characterize wave-WEC interaction, laboratory tests of a 1:30 WaveCat model are conducted using the two configurations and low-, mid- and high-energy sea states characteristic of the study area. The reflection and transmission coefficients obtained from the laboratory tests are inputted into a suite of numerical models to investigate the hydro- and morphodynamics of the beach. We find that the smaller wedge angle (30°) WECs afford more (less) coastal protection - quantified in terms of dry beach area availability - for short (long) peak periods than WECs with 60° . These results allow us to conclude that, for optimum performance of dual wave farms, WEC geometry should be adapted dynamically to the sea state.

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Keywords: Ocean energy; wave farm; laboratory experiments; numerical modelling; device design

1. Introduction

The development of renewable energy is one of the most relevant targets confronting society in the coming decades [1, 2], due to the finite nature of fossil fuels, their high costs and, last but not least, the environmental impacts of their exploration and use [3, 4]. Among the carbon-free energy sources, marine energy resources offer a vast potential and comparatively low effects on the environment [5–9]. In particular, the worldwide potential of wave energy was assessed as 17 TW h/year [10]. These facts contrast with the low degree of development and utilization of wave energy compared to other renewable sources, such as hydroelectric, biomass or wind energy [11, 12].

For these reasons, increasing research efforts have focused on wave energy over the last years. The objectives of the investigations carried out so far have been: (1) the assessment and characterization of wave energy resources [13–25], (2) the study and optimization of possible locations [26–33], (3) the economic viability of wave energy [34–38], (4) the combined implementation with other ocean energies, most notably, wind [39–44], and (5) the development of wave energy technologies and devices [23, 45–63, 63–75].

One of the wave energy converters (WECs) under development is WaveCat [13, 76]. A floating, overtopping WEC, it comprises two hulls joined at the stern by a hinge – for a detailed description of the device, the reader is referred to [48, 77]. Wave farms consisting of WaveCat WECs have been proven to fulfil a dual function as wave energy generators and coastal defence elements on both sandy beaches [78–81] and gravel-dominated coasts [82–86].

So far, the effects of the WEC configuration on the hydro- and morphodynamics of the coast in the lee of the wave farm have not been studied. The main objective of the present research is to analyse the effects of the configuration of WaveCat, in particular, the wedge angle or angle between the twin hulls, on

28 wave propagation, longshore sediment transport (LST) and shoreline dynamics,
 29 considering the varying transmission and reflection coefficients obtained from
 30 laboratory experiments under different sea states.

31 The laboratory experiments were conducted in the Ocean Basin of the Uni-
 32 versity of Plymouth (Section 3.1). In addition, this research involved the appli-
 33 cation of a wave propagation model (Section 3.2.1), an LST formulation (Sec-
 34 tion 3.2.2) and a one-line model (Section 3.2.3) to a study site in southern Spain
 35 (Section 2).

36 2. Study site

37 Playa Granada is a gravel-dominated deltaic beach located on the Mediter-
 38 ranean coastline of southern Spain (Figure 1a). The beach, which is bounded
 39 by the Guadalfeo River mouth to the west and by *Punta del Santo* to the east
 40 (Figure 1b), has been experiencing shoreline retreat and terminal erosion in re-
 41 cent years [87–89], partly due to anthropogenic interventions in the Guadalfeo
 42 River basin [90–92].

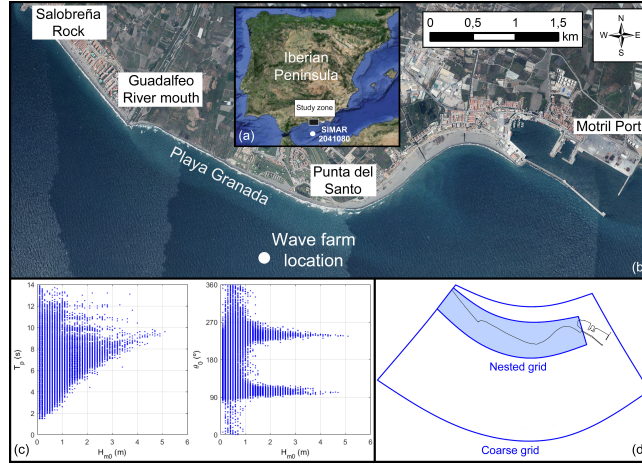


Figure 1: (a) Locations of the study zone and SIMAR point 2041080 in southern Iberian Peninsula. (b) Aerial image of the deltaic coast, indicating the wave farm location and the studied coastline section (Playa Granada). (c) Distributions $H_{m0}-T_p$ and $H_{m0}-\theta_0$ according to the SIMAR data. (d) Computational grids employed to apply the wave propagation model.

Two incoming wave directions are predominant at the study site (Figure 1c): south-west (SW) and south-east (SE). The values of deep-water significant wave height which are not exceeded 50%, 90%, 99% and 99.9% of the time are 0.5 m, 1.2 m, 2.1 m and 3.1 m, respectively [93]. The astronomical tidal range is ~ 0.6 m [94] and surge levels under storm conditions frequently exceed 0.5 m [95].

3. Methods

3.1. Laboratory experiments

Laboratory tests were performed in the Ocean Basin of the University of Plymouth to measure the reflection (K_r) and transmission (K_t) coefficients for two different wedge angles, i.e., angles between the hulls of WaveCat ($\alpha = 30^\circ$ and $\alpha = 60^\circ$, Figure 2). The experiments were carried out at a 1:30 scale and the dimensions of the model were 3 m (length) and 0.6 m (height) (Figure 2).

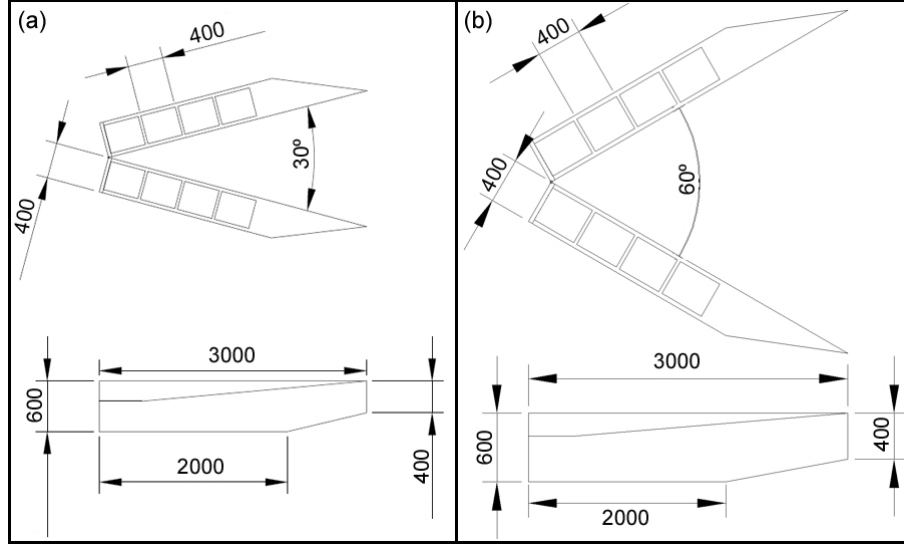


Figure 2: WEC configurations considered, model scale (dimensions in mm): (a) $\alpha = 30^\circ$, (b) $\alpha = 60^\circ$.

55 The selection of the two wedge angle values was done to represent two dif-
56 ferent types of operation of WaveCat corresponding to two different types of
57 sea state: one in which the length of the incoming wave front that is harnessed
58 by the device is maximised ($\alpha = 60^\circ$), given that the wave power per linear
59 metre of wave front is limited (low-energy sea state); and another in which the
60 amount of wave power per linear meter of wave front is substantial (high-energy
61 sea state), and therefore harnessing a shorter stretch of wave front is sufficient
62 to reach the rated power of the device ($\alpha = 30^\circ$).

63 Twelve different sea states were tested, with values of the significant wave
64 height (H_{m0}) between 0.03 m and 0.1 m (1 m and 3 m) in the model (prototype).
65 The tested values of the spectral peak period ($T_{p,mod}$) ranged from 1.28 s to 2.37
66 s, representing real values ($T_{p,prot}$) from 7 s to 13 s (Froude similarity). These
67 sea states are representative of the wave conditions in Playa Granada (Figure
68 1c). The tested sea states, along with the measured reflection and transmission
69 coefficients, are summarized in Table 1. A detailed description of the laboratory
70 experiments can be found in [96, 97].

71 3.2. Numerical modelling

72 3.2.1. SWAN model

73 The SWAN model was used to propagate the sea states in the prototype
74 scale, detailed in Section 3.1, from deep-water toward the coast for the two pre-
75 vailing directions at the study zone (Figure 1c): SW (238°) and SE (107°). The
76 model was previously calibrated for the study area by [98] through comparison
77 with field data.

78 The wave farm location, shown in Figure 1b, was selected based on the
79 results from previous studies, which have demonstrated that it is the best site
80 in terms of wave energy potential [28] and coastal protection [84]. The wave
81 farm layout, consisting of 11 WaveCat WECs spaced by a distance of 180 m
82 and arranged in two rows, was also chosen on the basis of recent works at the
83 study site [83, 85].

Test case	$H_{m0,mod}$	$H_{m0,prot}$ (m)	$T_{p,mod}$ (s)	$T_{p,prot}$ (s)	α (°)	K_r (-)	K_t (-)
S1_30	0.03	1	1.28	7	30	0.558	0.271
S2_30	0.03	1	1.64	9	30	0.436	0.368
S3_30	0.03	1	2.01	11	30	0.329	0.413
S4_30	0.03	1	2.37	13	30	0.268	0.441
S5_30	0.07	2	1.28	7	30	0.49	0.293
S6_30	0.07	2	1.64	9	30	0.399	0.363
S7_30	0.07	2	2.01	11	30	0.326	0.414
S8_30	0.07	2	2.37	13	30	0.266	0.439
S9_30	0.1	3	1.28	7	30	0.428	0.304
S10_30	0.1	3	1.64	9	30	0.361	0.359
S11_30	0.1	3	2.01	11	30	0.322	0.415
S12_30	0.1	3	2.37	13	30	0.265	0.437
S1_60	0.03	1	1.28	7	60	0.726	0.28
S2_60	0.03	1	1.64	9	60	0.499	0.359
S3_60	0.03	1	2.01	11	60	0.277	0.381
S4_60	0.03	1	2.37	13	60	0.213	0.387
S5_60	0.07	2	1.28	7	60	0.627	0.274
S6_60	0.07	2	1.64	9	60	0.351	0.342
S7_60	0.07	2	2.01	11	60	0.254	0.382
S8_60	0.07	2	2.37	13	60	0.186	0.399
S9_60	0.1	3	1.28	7	60	0.567	0.269
S10_60	0.1	3	1.64	9	60	0.399	0.336
S11_60	0.1	3	2.01	11	60	0.262	0.375
S12_60	0.1	3	2.37	13	60	0.189	0.396

Table 1: Wave conditions in the model ($H_{m0,mod}$, $T_{p,mod}$) and prototype ($H_{m0,prot}$, $T_{p,prot}$) scales, angle between hulls (α), reflection coefficient (K_r) and transmission coefficient (K_t) of the cases tested in the laboratory.

Two numerical grids were defined and used (Figure 1d): a coarse grid covering the entire deltaic region and extending from deep to shallow waters, and a nested grid covering the nearshore region, including the wave farm area, with higher resolution. To properly model the wave farm effects, the WECs were introduced in SWAN as artificial obstacles, specifying their reflection and transmission coefficients (hereafter denoted by K_r and K_t , respectively) for each sea state and wedge angle (Table 1). The results provided by SWAN were utilized to obtain wave variables at breaking conditions (through the fraction breaking variable) and, on this basis, apply the LST formulation below.

93 3.2.2. Longshore sediment transport formulation

94 LST was obtained through the formulation proposed by [99], which was
 95 found in previous work [98] to provide good estimates of the measured LST
 96 rates at the study site. The following expression was used:

$$Q = 0.00018K\rho_s g^{0.5} (\tan \beta)^{0.4} (d_{50})^{-0.6} (H_{m,br})^{3.1} \sin(2\theta_{br}), \quad (1)$$

97 where Q is the LST rate, ρ_s is the sediment density, g the gravity accelera-
 98 tion, $\tan \beta$ the beach slope of the surf zone, d_{50} the grain size, $H_{m,br}$ (θ_{br}) the
 99 breaking significant wave height (wave angle respect to shore-normal) and the
 100 coefficient K considers the effect of wave period on LST.

101 3.2.3. One-line model

102 The LST rates obtained with the equation of [99] and detailed in the previous
 103 section were used to calculate the changes in the shoreline position through the
 104 application of a one-line model [100], which is based on the following equation:

$$\frac{\partial y_s}{\partial t} = -\frac{1}{D} \left(\frac{\partial Q}{\partial x_s} \right), \quad (2)$$

105 where y_s and x_s are the coordinates of the shoreline, t is the time, and D
 106 is the sum of the height of the berm and the closure depth. [98] proved that
 107 the joint application of the SWAN model, the LST formulation of [99] and the
 108 one-line model replicates the coastline changes in Playa Granada.

109 4. Results

110 4.1. Significant wave heights at breaking

111 This section details the influence of the wave farm on wave propagation – in
 112 particular, on the significant wave heights at breaking – depending on the wedge
 113 of the WECs. The alongshore variation of the differences between breaking
 114 significant wave heights for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ ($\Delta H_{m,br}$) are indicated in
 115 Figure 3.

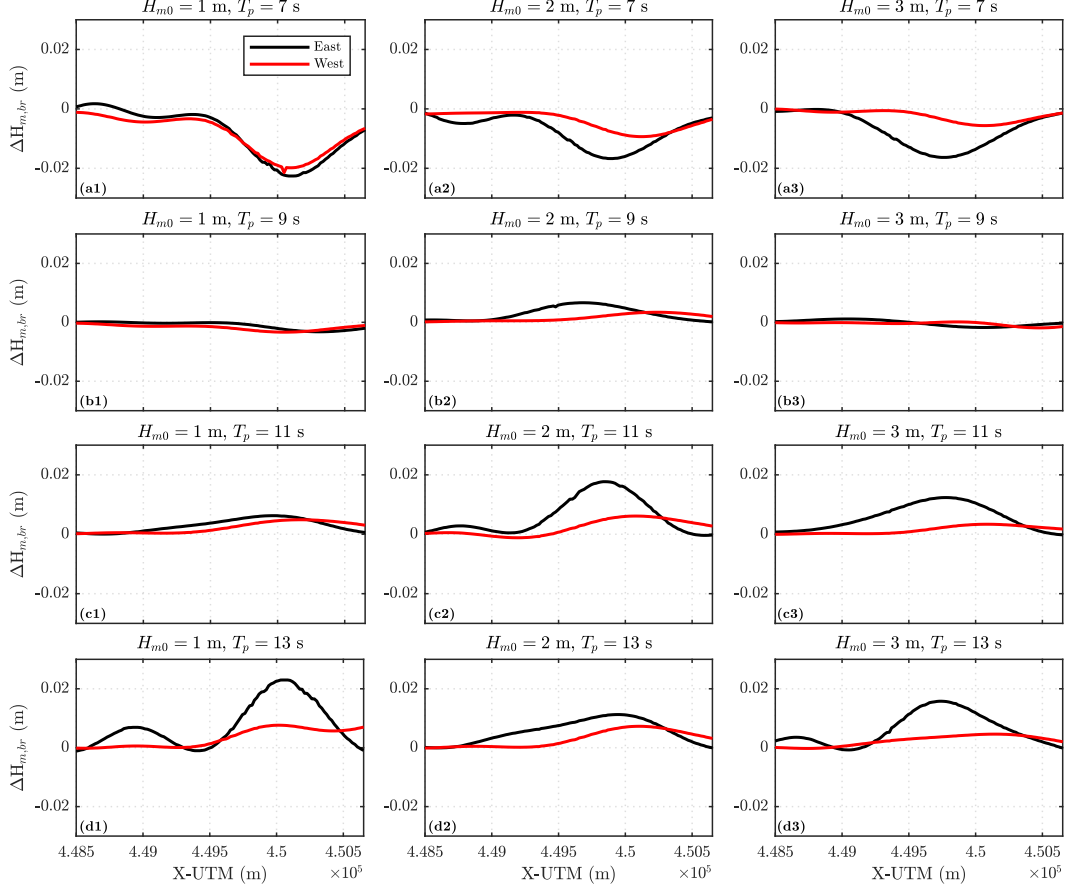


Figure 3: Alongshore distribution of the differences between the significant wave heights at breaking for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SW (red) and SE (black) waves. $[\Delta H_{m,br} = H_{m,br,30} - H_{m,br,60}]$.

Under SW waves, it is shown that the differences are generally negative for short wave periods ($T_p = 7$ s) and positive for long periods ($T_p = 11$ s and $T_p = 13$ s). In all the cases, the maximum differences are reached at the eastern part of the coast, influenced by the location of the wave farm (shown in Figure 1) and its effects in the leeward wave propagation patterns.

For all the H_{m0} , the alongshore-averaged values of $\Delta H_{m,br}$ for SW waves increase with increasing values of T_p (Figure 4). Thus, in terms of wave energy at the breaking zone, the wave farm composed by devices with the 30° config-

uration provides more (less) protection for short (long) T_p than that with the 60° configuration. This is a result of the different K_r and K_t of both configurations (Table 1). For given values of T_p , the differences in breaking wave heights between both angles decrease for increasing values of H_{m0} (Figure 4).

Under incoming SE waves, the differences are also negative (positive) for short (long) T_p , although in this case they extend along most of the study stretch (Figure 3). For constant values of H_{m0} , the alongshore-averaged $\Delta H_{m,br}$ under SE waves is greater for longer T_p (Figure 4); it is also due to the differences in K_r and K_t between both devices (Table 1). Thus, the greater the values of T_p , the lower the protection provided by devices with $\alpha = 30^\circ$ compared to those with $\alpha = 60^\circ$.

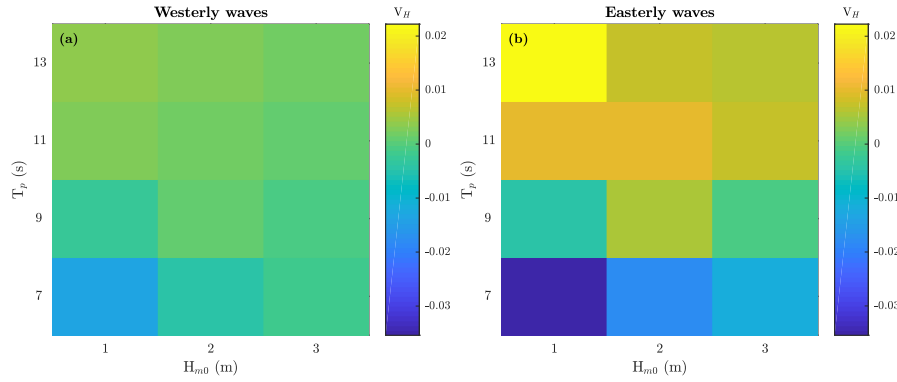


Figure 4: Variation in the alongshore-averaged significant wave heights at breaking for $\alpha = 30^\circ$ with respect to the values for $\alpha = 60^\circ$ under SW (a) and SE (b) waves. $[V_H = (\bar{H}_{m,br,30} - \bar{H}_{m,br,60})/\bar{H}_{m,br,30}]$.

The differences in significant wave height at breaking between both devices under SE wave conditions are generally greater than those under SW waves (Figure 4); with maximum negative (positive) alongshore-averaged values of $\Delta H_{m,br}$ equal to -0.82 cm (0.77 cm) for low-energy waves ($H_{m0}=1$ m), -0.77 cm (0.55 cm) for mid-energy waves ($H_{m0}=2$ m), and -0.71 cm (0.61 cm) for high-energy waves ($H_{m0}=3$ m).

4.2. Longshore sediment transport rates

The differences in LST rates between the WECs with $\alpha = 30^\circ$ and $\alpha = 60^\circ$ are analysed in this section. Figure 5 depicts the alongshore distribution of these differences for all the sea states considered. Under SW waves, the differences are generally greater for higher values of $H_{m,0}$ and lower values of T_p , i.e. the greater the wave steepness, the higher the differences in LST rates between the farms with both angles. The differences are more significant in the western (eastern) stretch of the coast for short (long) peak periods (Figure 5).

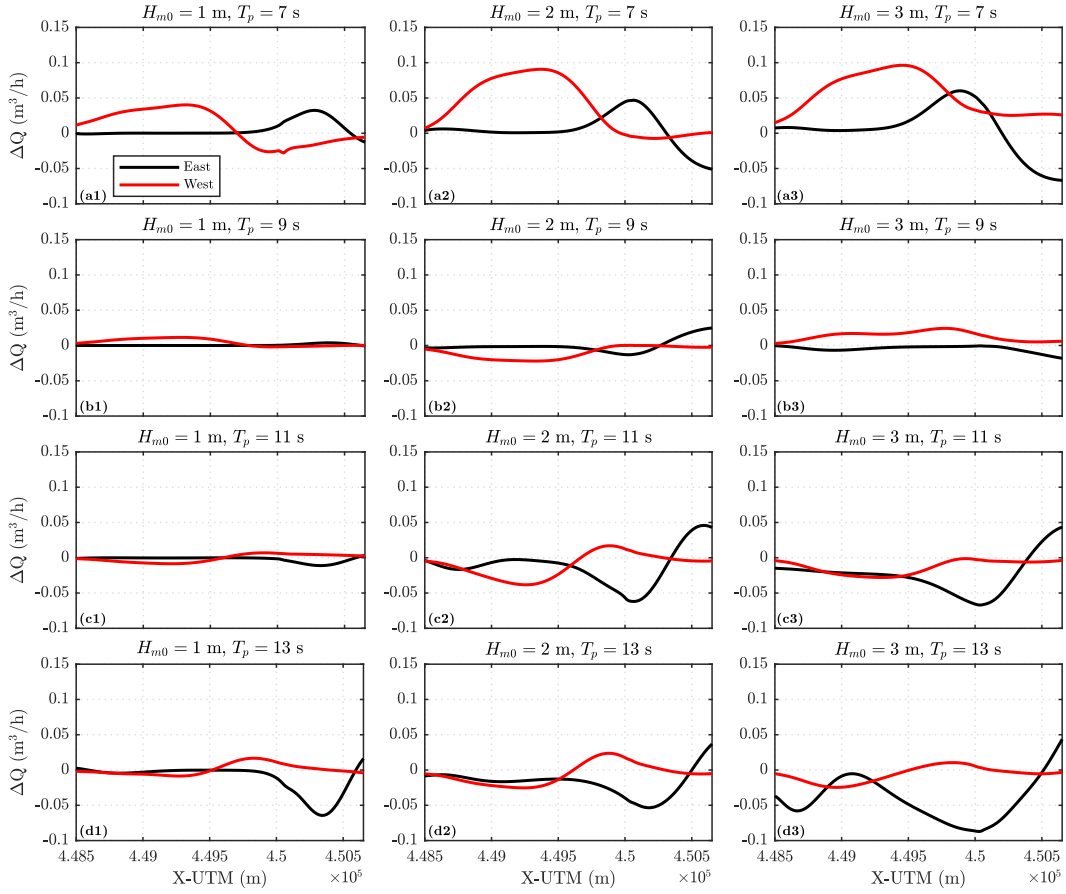


Figure 5: Alongshore distribution of the differences between the LST rates for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SW (red) and SE (black) waves. $[\Delta Q = Q_{30} - Q_{60}]$.

Under SE wave conditions, the greater differences are located in the eastern

part of the study section (Figure 5), i.e., in the lee of the wave farm (Figure 1). For short periods ($T_p = 7$ s), the differences are negative in the eastern end of the stretch of beach and become positive toward the west; whereas the opposite occurs for long periods ($T_p = 11$ s and $T_p = 13$ s). In general, the differences are greater as the $H_{m,0}$ values increase (Table 2).

	SW waves			SE waves		
	$H_{m0}=1$ m	$H_{m0}=2$ m	$H_{m0}=3$ m	$H_{m0}=1$ m	$H_{m0}=2$ m	$H_{m0}=3$ m
$T_p=7$ s	-0.0092	-0.0385	-0.0548	-0.0055	-0.0052	-0.0073
$T_p=9$ s	-0.0045	0.0105	-0.0136	-0.0006	0.001	0.0044
$T_p=11$ s	0.0006	0.0104	0.0134	0.002	0.0128	0.0256
$T_p=13$ s	-0.0007	0.0054	0.0062	0.0116	0.0185	0.0425

Table 2: Differences between the alongshore-averaged LST rates for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SW and SE waves (in m^3/h).

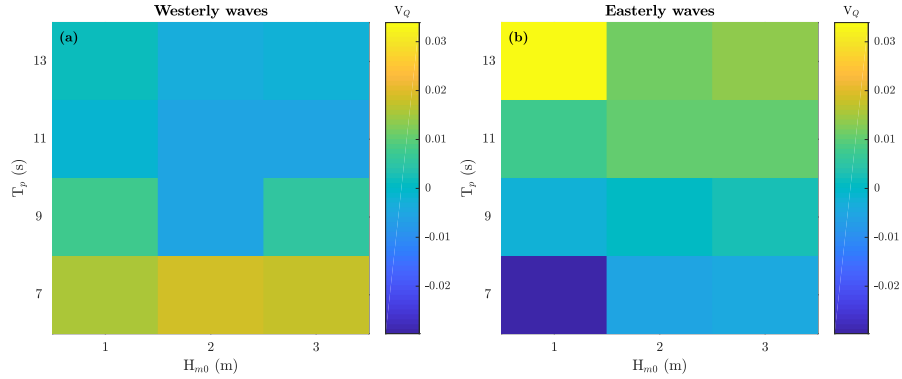


Figure 6: Variation in the alongshore-averaged LST rates for $\alpha = 30^\circ$ with respect to the values for $\alpha = 60^\circ$ under SW (a) and SE (b) waves. $[V_Q = (\bar{Q}_{30} - \bar{Q}_{60})/\bar{Q}_{30}]$.

The differences in LST rates between the farms composed by both devices under SE wave conditions are greater than those under SW waves (Table 2 and Figure 6). This is influenced by both the higher differences in breaking significant wave heights (Section 4.1) and the higher angles from shore-normal for SE waves, which increase the LST rates and differences.

4.3. Shoreline geometry

The LST rates obtained in the previous section were used to compute the variations in the shoreline morphology over a one-month period for $H_{m,0}=1$ m, $H_{m,0}=2$ m and $H_{m,0}=3$ m, representing low-, mid- and high-energy conditions, respectively. The differences between the final shorelines for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under both SW and SE waves are shown in Figure 7.

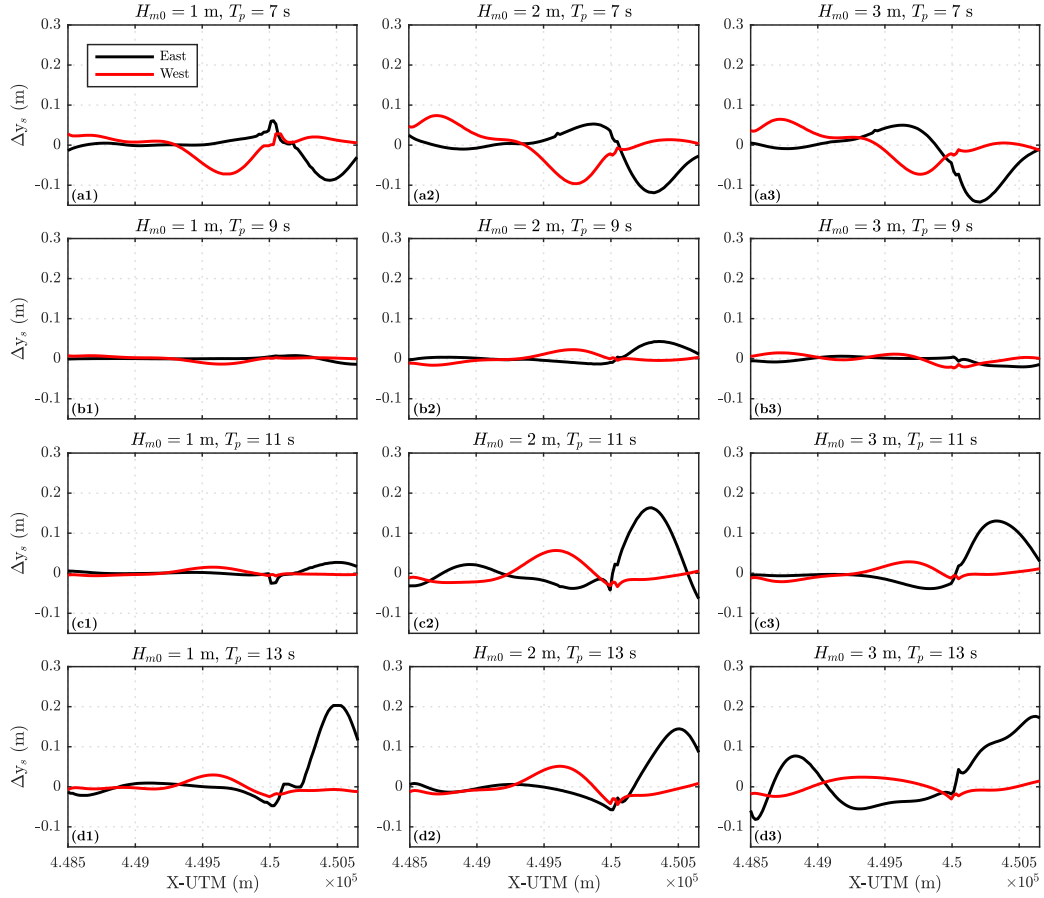


Figure 7: Alongshore distribution of the the differences between the final coastline positions (after 1 month) for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SW (red) and SE (black) waves. $[\Delta y = y_{\text{final},30} - y_{\text{final},60}]$.

For SW waves and short peak periods ($T_p=7$ s), the maximum differences are negative and concentrated in the central stretch of beach (where the main

occupations are located), indicating that the wave farm with $\alpha = 30^\circ$ provides greater protection at this location. On the contrary, the differences in the western part of the beach are positive (Figure 7), i.e., the farm with $\alpha = 60^\circ$ leads to greater accretion near the river mouth for short wave periods. This section has experienced acute shoreline retreat in recent years due to river damming [91].

For long wave periods ($T_p=11$ s and $T_p=13$ s), the maximum differences under SW waves are positive and located in the central stretch of beach. In addition, the alongshore-averaged values are positive for low-, mid- and high-energy conditions (Table 3). Thus, under SW waves with long periods, the wave farm with $\alpha = 60^\circ$ provides greater protection against shoreline erosion. This leads to a higher efficiency in terms of dry beach area (Section 4.4).

	SW waves			SE waves		
	$H_{m0}=1$ m	$H_{m0}=2$ m	$H_{m0}=3$ m	$H_{m0}=1$ m	$H_{m0}=2$ m	$H_{m0}=3$ m
$T_p=7$ s	-0.36	-0.06	0.21	-0.66	-1.06	-1.65
$T_p=9$ s	-0.04	-0.04	0.02	0.01	0.54	0.39
$T_p=11$ s	0.05	0.05	0.01	0.3	1.65	1.48
$T_p=13$ s	0.1	0.06	0.03	2.1	1.23	2.01

Table 3: Differences between the alongshore-averaged final coastline positions for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SW and SE waves (in cm).

On the other hand, under SE waves, the greatest differences are concentrated along the eastern section of the coastline. This is caused by the farm location (Figure 1) and the resulting greater differences in LST between both angles at this stretch of beach (Figure 5). The differences in final shoreline positions are generally negative (positive) for short (long) peak periods, indicating that the wave farm composed by WECs with $\alpha = 30^\circ$ ($\alpha = 60^\circ$) provides more protection for short (long) wave periods (Figure 5 and Table 3).

For all the sea states considered, the differences in the final shoreline geometries between devices with $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SE wave conditions are higher than those under SW waves. These differences determine the dry beach area availability, as explained in the following section.

191 4.4. Dry beach area

192 The differences between the final and initial dry beach areas for all the sea
 193 states analysed and for both angles between the hulls are depicted in Figure 8. It
 194 may be observed that these differences are always positive, i.e., beach accretion
 195 occurs in all cases. This confirms the efficiency of wave farms as protection
 196 elements against coastline erosion.

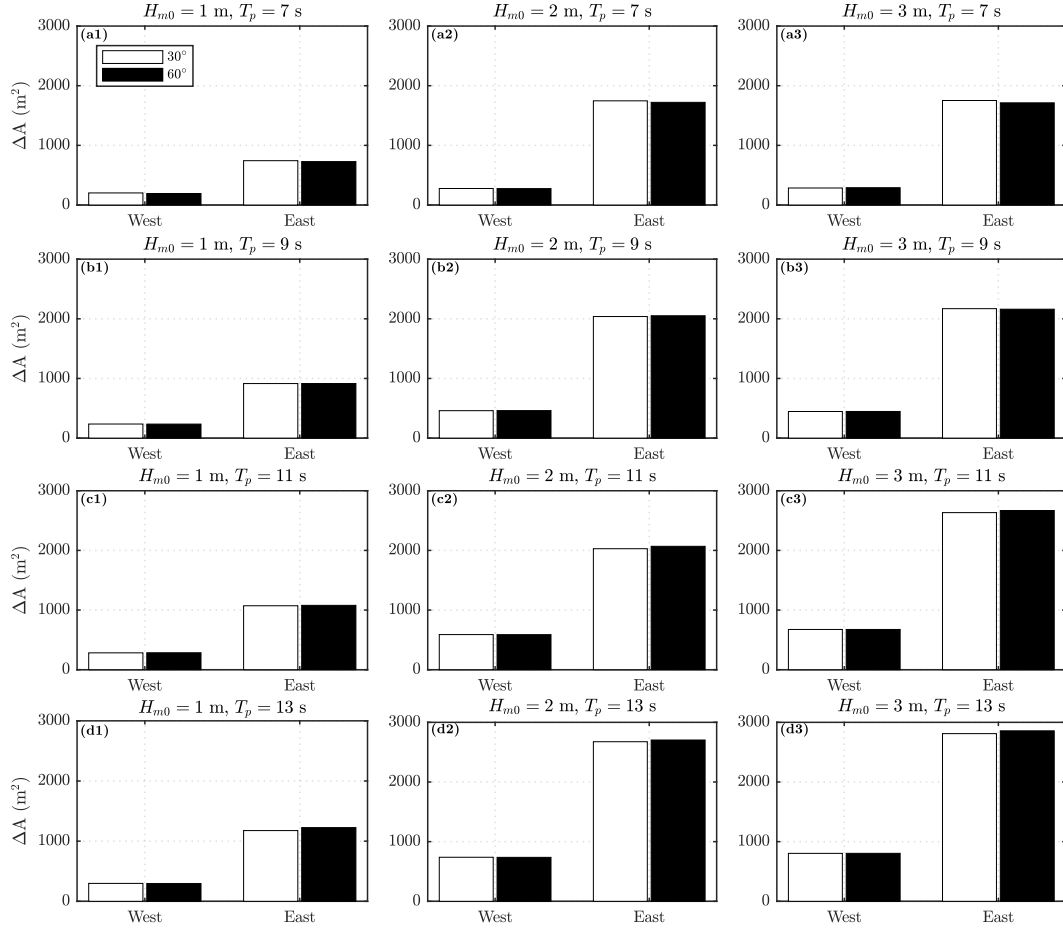


Figure 8: Dry beach area variations for $\alpha = 30^\circ$ (white) and $\alpha = 60^\circ$ (black) under SW and SE waves. $[\Delta A = A_{\text{final}} - A_{\text{initial}}]$.

As shown in Figure 8, the accretion is more pronounced under SE waves. This is in agreement with the observed morphological response of the coastline, since SW waves contribute to erode the beach and SE waves lead to beach recovery [98, 101]. In this case, the presence of the farm increases the beach accretion under SE waves and reverts the coastline response (from erosion to accretion) under SW wave conditions. The dry beach area differences are generally greater with increasing values of H_{m0} and T_p (Figure 8).

The comparison of the results obtained for both angles between hulls allow concluding that, under SW waves, the farm composed by devices with $\alpha = 60^\circ$ is more efficient in terms of coastal protection for all the cases except four of them (associated to mild conditions): $H_{m0}=1$ m - $T_p=7$ s, $H_{m0}=1$ m - $T_p=9$ s, $H_{m0}=2$ m - $T_p=7$ s and $H_{m0}=2$ m - $T_p=9$ s (Table 4 and Figure 9). Under SE waves, the WaveCat devices with $\alpha = 30^\circ$ are more efficient for the shortest peak period ($T_p=7$ s), whereas those with $\alpha = 60^\circ$ lead to greater accretion values for the rest of wave conditions (Table 4).

	SW waves			SE waves		
	$H_{m0}=1$ m	$H_{m0}=2$ m	$H_{m0}=3$ m	$H_{m0}=1$ m	$H_{m0}=2$ m	$H_{m0}=3$ m
$T_p=7$ s	9.4	1.8	-4.7	15.4	26	39
$T_p=9$ s	1	0.9	-0.5	-0.5	-13	-9
$T_p=11$ s	-1.3	-1.1	-0.1	-7	-41	-36
$T_p=13$ s	-2.3	-1.4	-0.7	-49	-29	-47

Table 4: Differences between the final dry beach area for $\alpha = 30^\circ$ and $\alpha = 60^\circ$ under SW and SE waves (in m^2).

The results of this section indicate that, for the best performance in terms of coastal protection, the geometry of the WECs should be adjusted dynamically to the sea state. If this is not possible, i.e., if a fixed configuration (constant wedge angle) must be adopted, then this configuration should be chosen on the basis of a detailed analysis of the wave climate at the site of interest, with a view to optimizing the coastal protection performance under the prevailing sea states.

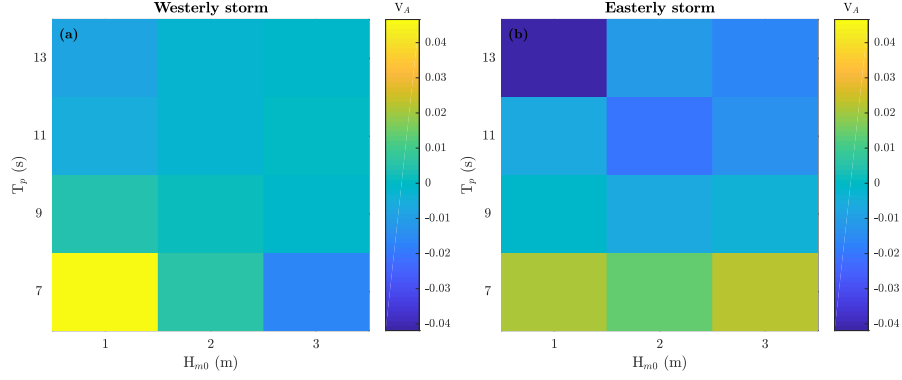


Figure 9: Variation in the dry beach area differences for $\alpha = 30^\circ$ with respect to the values for $\alpha = 60^\circ$ under SW (a) and SE (b) waves. $[V_A = (\Delta A_{30} - \Delta A_{60})/\Delta A_{30}]$.

219 The methodology presented in this work, which combines laboratory tests
 220 with different WEC configurations and numerical modelling, may be used for
 221 other geometries and beaches to investigate the optimum configuration for a
 222 wave farm project.

223 5. Conclusions

224 Wave energy is one of the renewables with the greatest potential for develop-
 225 ment due to the resource availability and low visual pollution. Recent research
 226 has highlighted the possibility of using wave farms for a dual function, i.e.,
 227 renewable energy generation and coastal protection.

228 This paper presents the first study on the influence of WEC configuration
 229 on the performance of dual wave farms. In particular, the effects of two values
 230 of the wedge angle, i.e., the angle between the twin hulls of WaveCat WECs
 231 ($\alpha = 30^\circ$ and $\alpha = 60^\circ$) on significant wave height at breaking, LST rates,
 232 shoreline geometry and dry beach area were analysed. For this purpose, the
 233 transmission and reflection coefficients were determined for relevant sea states
 234 based on laboratory experiments in a wave tank, and these values were used to
 235 model the wave farm-induced morphological variations on a gravel-dominated
 236 beach.

237 The results indicate that, under both SW and SE waves, the wave farm
238 composed by WaveCat devices with $\alpha = 30^\circ$ provides more (less) protection for
239 short (long) peak periods, quantified in terms of breaking wave heights. This
240 is down to the different values of the transmission and reflection coefficients
241 corresponding to the two configurations. The differences in significant wave
242 height at breaking between the two WEC configurations under SE waves are
243 generally greater than those under SW waves. This, along with the more oblique
244 incidence for SE waves, leads to greater differences in LST rates between the
245 two configurations under SE waves.

246 The LST rates thus obtained were used to compute the changes in shoreline
247 geometry and dry beach area. The results confirm the efficiency of wave farms in
248 coastal protection indeed, accretion occurs under all the sea states considered.
249 The gains in dry beach area obtained with the 60° WEC configuration were
250 generally greater for long peak periods ($T_p=11$ s and $T_p=13$ s) and lower for
251 the shortest peak period ($T_p=7$ s). We conclude that the performance of dual
252 wave farms depends on both the WEC configuration and the sea state. In other
253 words, the optimum configuration depends on the sea state.

254 Therefore, for maximum performance of the wave farm in coastal erosion
255 protection, the WEC geometry should be adjusted dynamically to the sea state.
256 This dynamic adaptation strategy leads to a greater dry beach area. With
257 the methodology presented in this paper, this benefit may be quantified for
258 any beach of interest, and compared with the cost of the dynamic adaptation
259 strategy versus a constant geometry strategy in order to establish which is more
260 appropriate. Future research should focus on the assessment of the role of WEC
261 configuration in power production, investigating the optimum pair angle-draft
262 that maximises power production.

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